

Engineering Hydrology

Class 9

Infiltration: Horton Method

If you've not viewed it already, pause this webcast and open up the video under Lecture 8, a student-created video that illustrates a demonstration of infiltration. The student authors are Cui, Dearing, Lyons and Martin.

Objectives

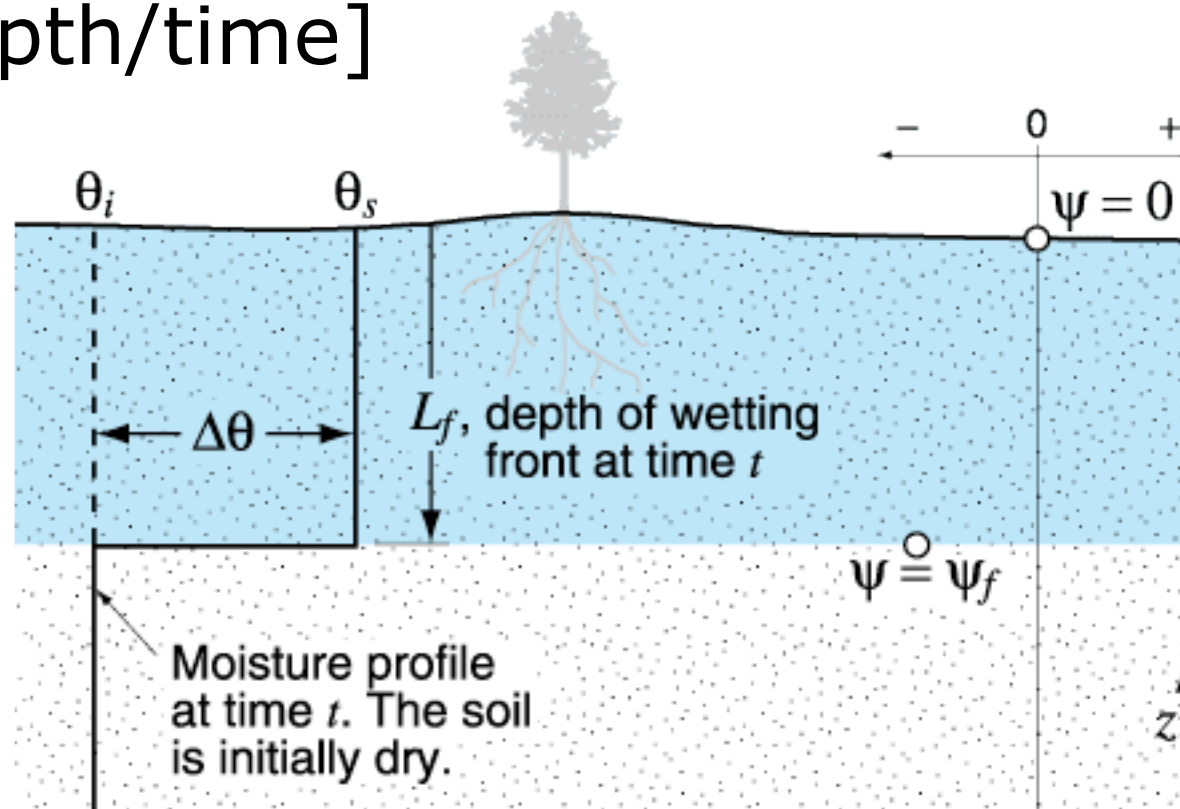
- Apply the Horton Method to estimate wetting front depth over time
- estimate aggregate amount of infiltration

Objectives

- Apply the Horton Method to estimate wetting front depth over time
- estimate aggregate amount of infiltration

Conditions of infiltration

- $P(t)$: precip event (rainfall and snow)
[depth/time]



Note:

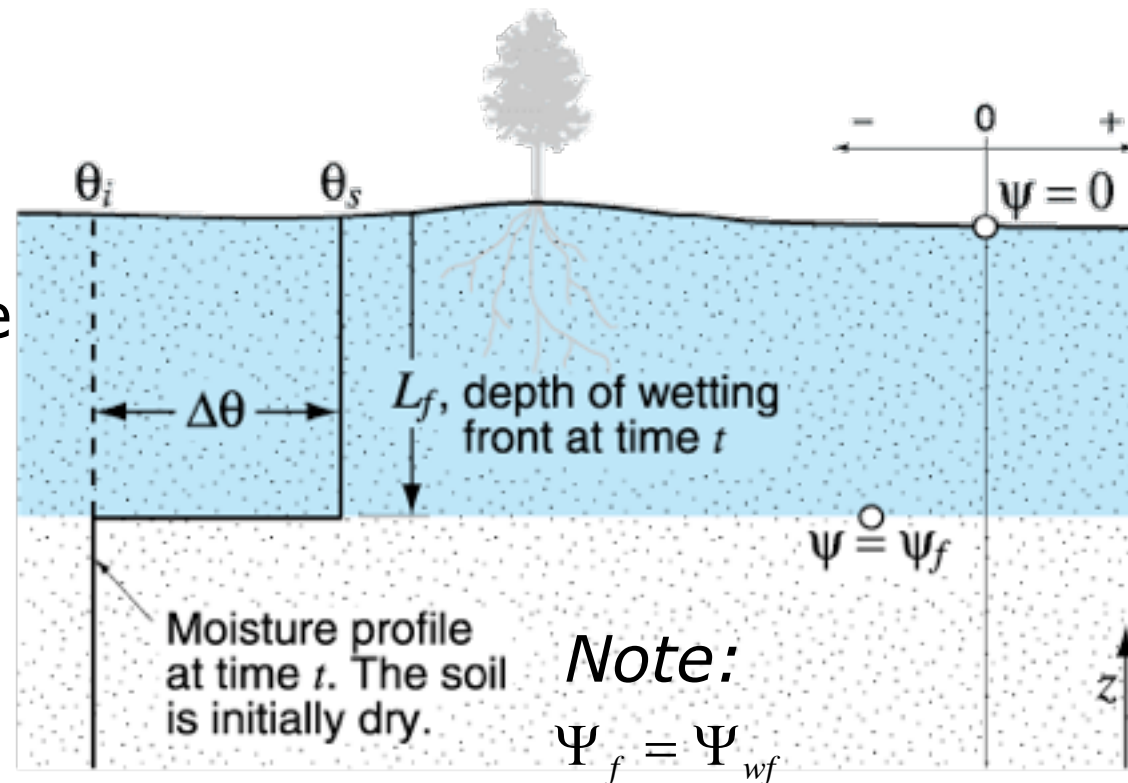
$$\Psi_f = \Psi_{wf}$$

and

$$L_f = L_{wf}$$

Conditions of infiltration

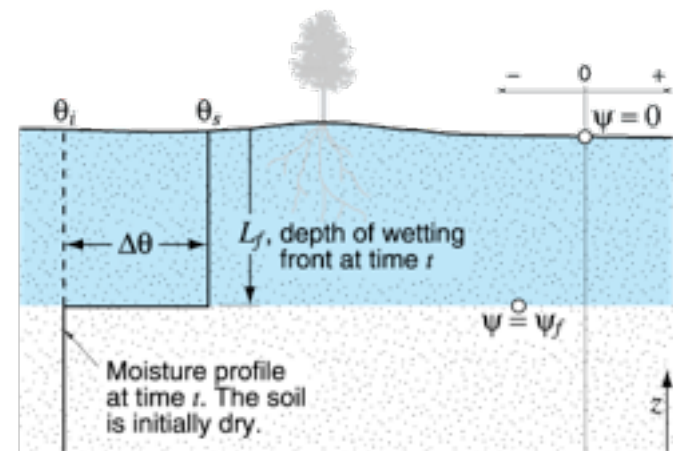
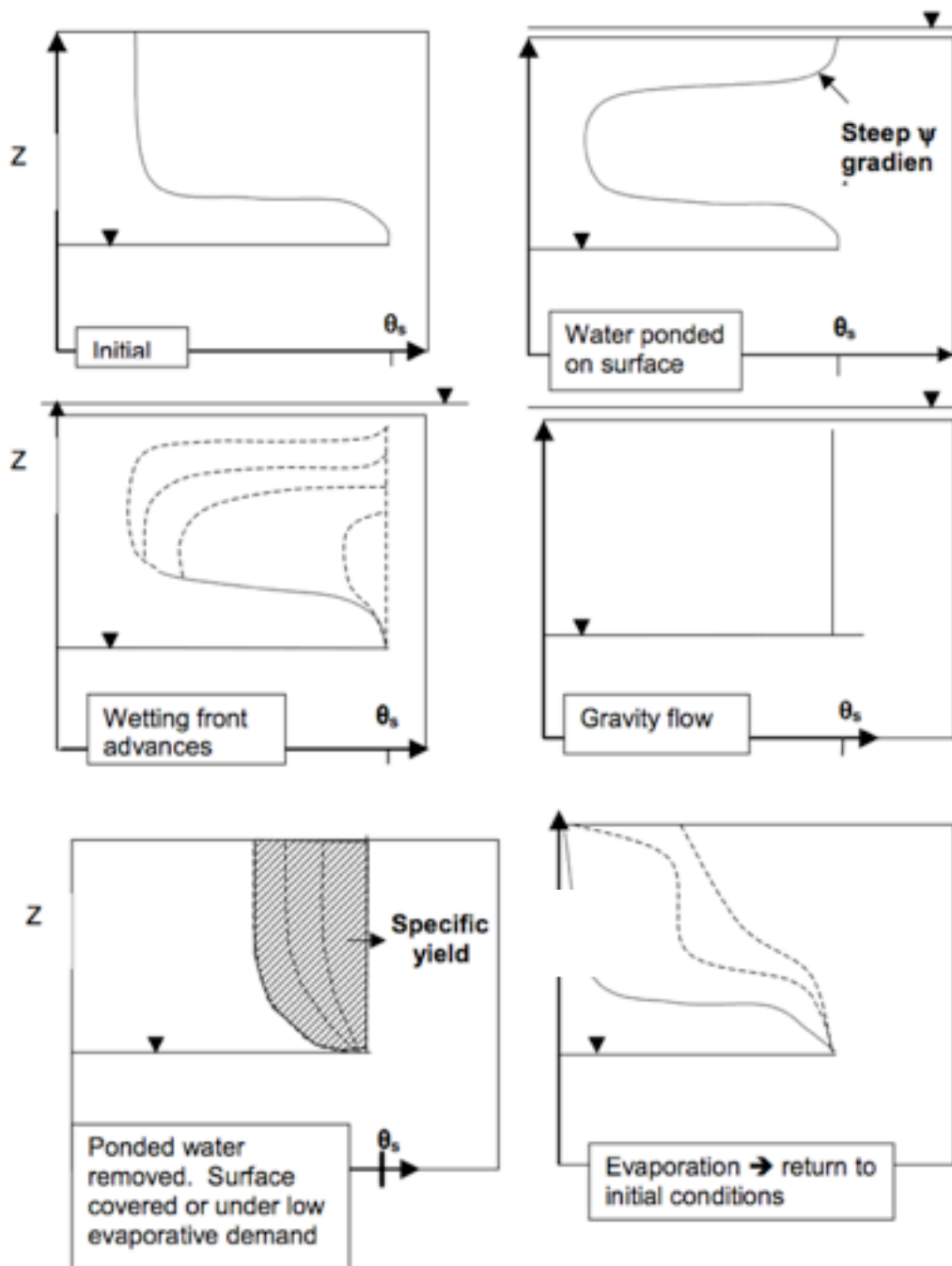
- $P(t)$: precip event (rainfall and snow) [depth/time]
- $f(t)$: infiltration rate [depth/time]
- $H(t)$: the depth of ponding
- $L(t)$: depth of wetting front
- Infiltration occurs under ponded or non-ponded conditions



and

$$L_f = L_{wf}^5$$

Process of Infiltration [Note: Y axes = Z (depth); X axes = θ]



Conditions of infiltration

(1) No ponding (water has not accumulated on the soil surface)

$$H(t)=0, f(t)=P(t)$$

Infiltration rate is equal to precip rate

(2) Surface ponding

$$H(t)>0, f(t)=f_{\max}(t)<P(t)$$

(3) Surface ponding (Overland flow)

$$H(t)>0, f(t)=0$$

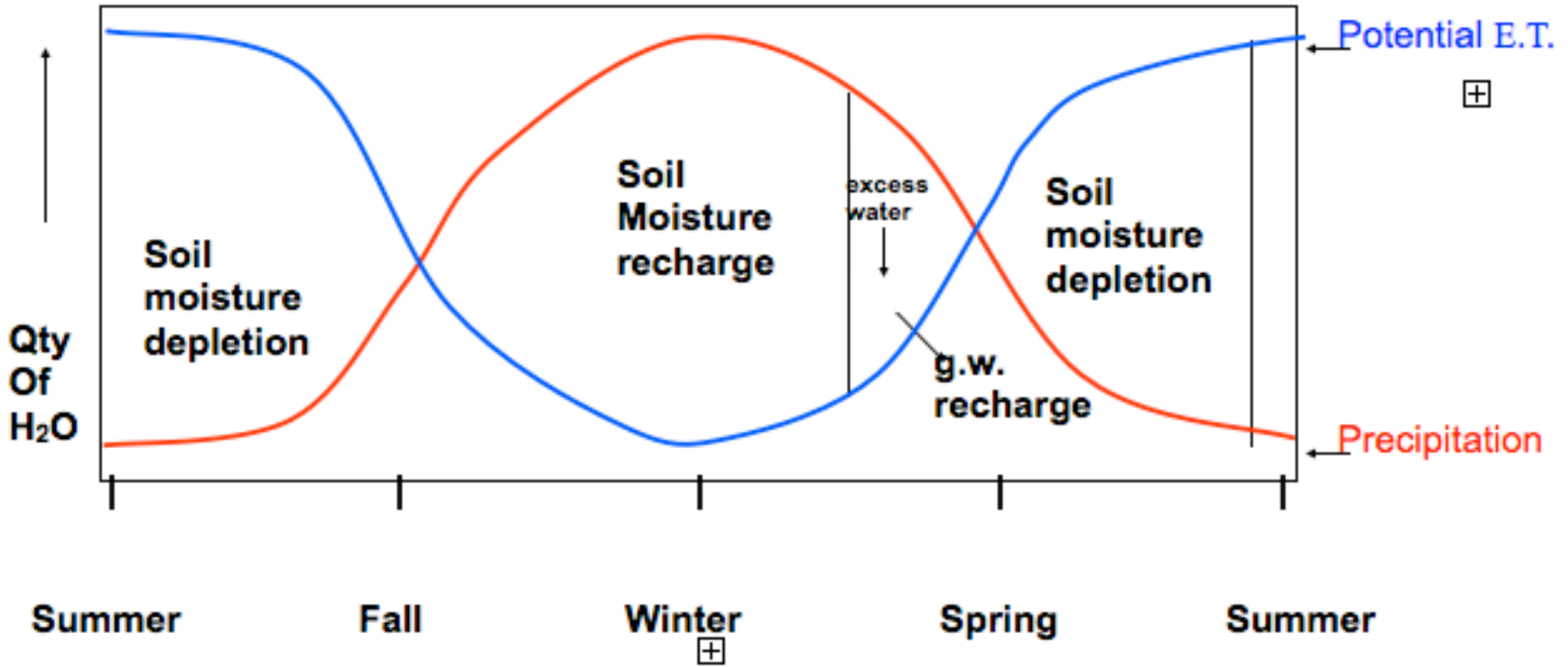
Infiltration Under Various Climatic Regimes

Humid climate:

- precipitation in all seasons
- virtually all non-discharge areas are ground water recharge areas
- recharge occurs at all seasons

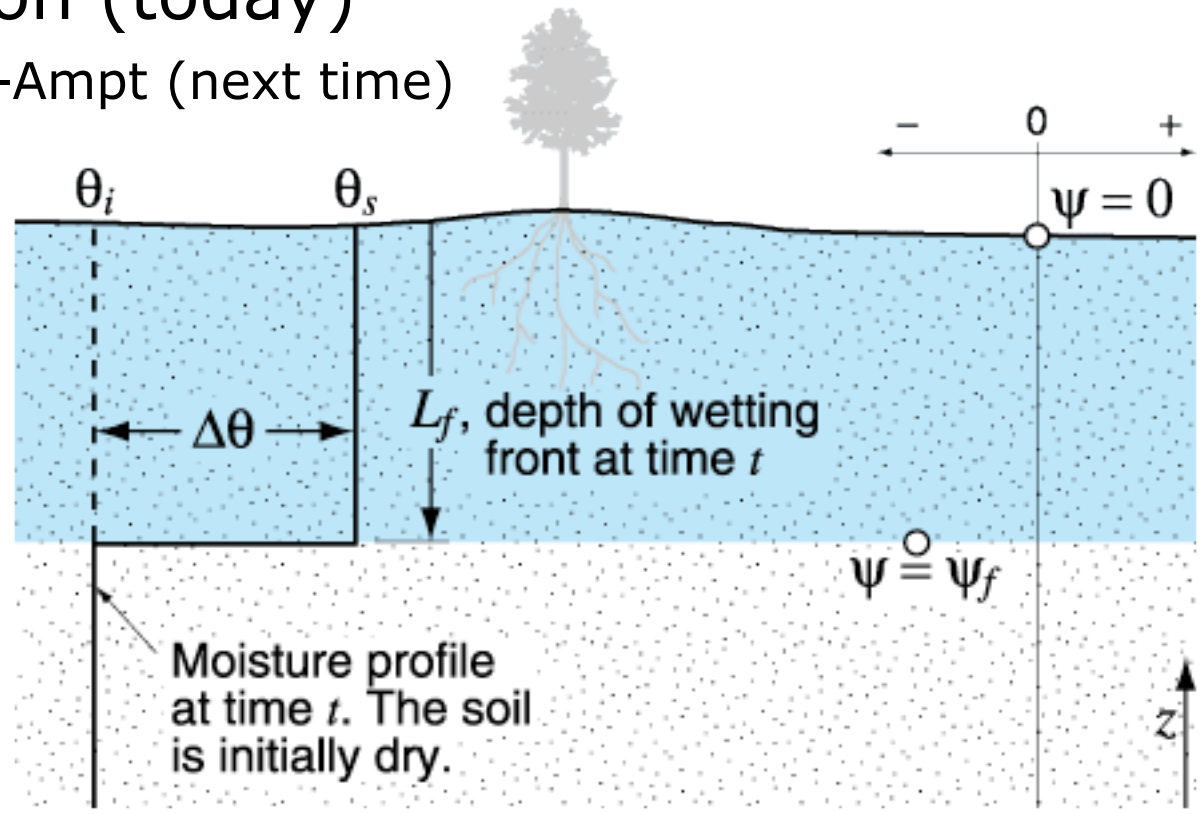
Humid to semi-humid climate – winter precipitation

Water balance of vadose zone



Methods we will examine:

- Horton (today)
- Green-Ampt (next time)



Note:

$$\Psi_f = \Psi_{wf}$$

and

$$L_f = L_{wf}$$

Another approach: Phi-index method
(reading material to be provided)

Horton method (1940)

- Maximum possible infiltration rates (f)
- Infiltration rate decreases with time after the onset of rainfall and ultimately reaches a constant rate (f_c)
- If at any time the rate of rainfall exceeds the infiltration capacity, excess water will pond on the soil surface (then overland flow)

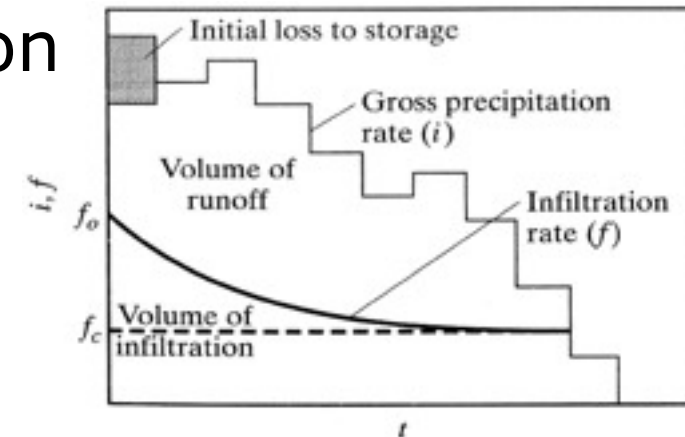


Figure 1-21

Horton method (1940)

$$f = f_c + (f_o - f_c)e^{-kt}$$

f : infiltration rate {length/time}

f_c : final infiltration rate

f_o : initial infiltration rate

k : decay parameter (a soil property)

f_c is equivalent to saturated hydraulic conductivity

Horton method (1940)

$$f = f_c + (f_o - f_c)e^{-kt}$$

Table 1-6. Typical Values of the Parameters of f_o , f_c , and k of the Horton Model

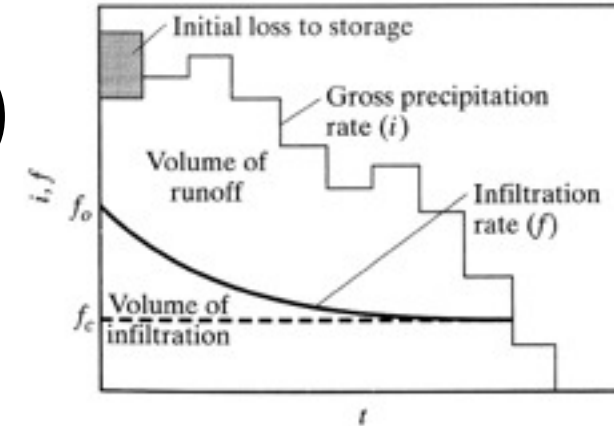
| Soil Type | f_c (in./hr) | f_o (in./hr) | k (hr ⁻¹) |
|--------------------------|-------------------|-------------------|----------------------------|
| Alphalpha loamy sand | 1.40 | 19.00 | 38.29 |
| Carnegie sandy loam | 1.77 | 14.77 | 19.64 |
| Dothan loamy sand | 2.63 | 3.47 | 1.40 |
| Fuquay pebbly loamy sand | 2.42 | 6.24 | 4.70 |
| Leefield loamy sand | 1.73 | 11.34 | 7.70 |
| Tooup sand | 1.80 | 23.01 | 32.71 |

After Rawls et al., 1976.

Horton method (1940)

Infiltration rate

$$f = f_c + (f_o - f_c)e^{-kt}$$



Cumulative infiltration volume ($F(t)$)

$$F(t) = \int f(t) dt \quad (\text{integrate above equation})$$

$$F(t) = f_c t + \left[\frac{f_o - f_c}{k} \right] (1 - e^{-kt})$$

Assumptions

- Assumes ponding conditions ($P(t) > 0$)
- Infiltration rate decrease as a function of time
- After a certain period, infiltration rate becomes constant (at this condition, $f_c = K_{\text{sat}}$ - the value of conductivity for saturated flow)

