**Engineering Hydrology** 

# Class 16: Direct Runoff (DRO) and Unit Hydrographs

#### **Topics and Goals:**

- 1. Calculate volume of DRO from a hydrograph;
- 2. Complete all steps to develop a Unit Hydrograph.



Class 14: Unit Hydrographs

Learning Objectives

Hydrograph Anatomy (components)

What is the Unit Hydrograph?

How do you construct the Unit HG?

Calculating Direct Runoff (DRO)



Class 14: Unit Hydrographs

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Calculating Direct Runoff (DRO)



- Duration of rainfall excess (D): time from start to finish of rainfall excess
- Lag time (L or  $t_p$ ) : time from the center of mass of rainfall excess to the peak of the hydrograph
- Time of rise  $(T_R)$ : time from the start of rainfall excess to the peak of the hydrograph
- Time of concentration  $(t_c)$ : time for a wave (of water) propagate from the most distant pt in the watershed to the outlet. One estimate is time from the end of net rainfall to the inflection pt.
- Time base  $(T_b)$ : total duration of the DRO hydrograph

Example: Develop Unit Hydrograph

Calculating

Direct Runoff (DRO)

# Unit Hydrograph

Hydrologic Analysis

Sherman (1932) originally advanced the theory of the unit hydrograph (UH), defined as "basin outflow resulting from 1.0 inch (1.0 mm) of direct runoff generated uniformly over the drainage area at a uniform rainfall rate during a specified period of rainfall duration." An important point here is that UH is composed of
1.0 inch of direct runoff, which is equivalent to 1.0 inch of net rainfall for a given duration, *D*, and therefore all losses to infiltration must be subtracted before computations. Several assumptions inherent in the unit hydrograph approach tend to limit its application for any given watershed (Johnstone and Cross, 1949):

- Rainfall excesses of equal duration are assumed to produce hydrographs with equivalent time bases regardless of the intensity of the rain.
- Direct runoff ordinates for a storm of given duration are assumed directly proportional to rainfall excess volumes. Thus, twice the rainfall produces a doubling of hydrograph ordinates.
- The time distribution of direct runoff is assumed independent of antecedent precipitation.
- Rainfall distribution is assumed to be the same for all storms of equal duration, both spatially and temporally.

Assume linear response

Example: Develop Unit Hydrograph

UNIT HYDROGRAPH THEORY Hydrograph Anatomy (components)

What is the Unit Hydrograph?

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Calculating Direct Runoff (DRO)





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Class 14: Unit Hydrographs

> Learning Objectives

From your text (BHV, p. 117):

The following are the essential steps for developing a unit hydrograph from a single storm hydrograph (see Fig. 2–7 and Example 2–3):

- Analyze the hydrograph and separate base flow (Section 2.3).
- 2. Measure the total volume of DRO under the hydrograph and convert this to inches (mm) over the watershed.
- Convert total rainfall to rainfall excess through infiltration methods, such that rainfall excess = DRO, and evaluate duration D of the rainfall excess that produced the DRO hydrograph.
- 4. Divide the ordinates of the DRO hydrograph (Fig. 2–7) by the volume in inches (mm) and plot these results as the unit hydrograph for the basin (Fig. 2–7). The time base  $T_b$  is assumed constant for storms of equal duration and thus it will not change.
- Check the volume of the unit hydrograph to make sure it is 1.0 in. (1.0 mm), and graphically adjust ordinates as required.

Class 14: Unit Hydrographs

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#### **Separating Baseflow**



Class 14: Unit Hydrographs

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### Volume (depth) of DRO?

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Class 14: Unit Hydrographs

Learning Objectives

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Calculating Direct Runoff (DRO)

#### In-Class Exercise: Volume (depth) of DRO?

*Use DRO hydrograph to calculate volume of DRO; one approach is the "trapezoidal rule" -- see E2-1(d) in handout (posted)* 

Class 14: Unit Hydrographs

> Learning Objectives

Hydrograph

Develop Unit Hydrograph

	Time (hr)	Q (cfs)	Volume (cfs-hr)	Anatomy (component
	0-2	100	200	(component
	2-4	300	600	What is the
700	4-6	500	1000	Unit
600	6-8	700	1400	Hydrograph
	8-10	650	1300	
5 200 F 171 1 17	10-12	600	1200	How do you
○ 400 - /       N	12-14	500	1000	construct th
300 - 1 - 1 - 1 - 1 - 1 - 1	14-16	400	800	Unit HG?
200 - /	16-18	300	600	
	18-20	200	400	Calculating
1007-	20-22	150	300	Direct Runo
	22-24	100	200	(DRO)
0 4 8 12 16 20 24	24-26	50	100	
Time (hr)	and the second s	I - I - I - I - I - I - I - I - I - I -	Contraction of the second second second	Example:

For a 2600-acre basin, what is the amount (depth) of DRO? Hints: (a) sum up the total volume in cfs-hour; (b) 1 cfs = 1 ac-in / hour

From BHV, p. 117:

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Class 14: Unit Hydrographs

Learning Objectives

Hydrograph Anatomy (components)

What is the Unit Hydrograph?

How do you construct the Unit HG?

Calculating Direct Runoff (DRO)



The phi-index is an assumed uniform and constant infiltration rate. It's calculated by finding the loss difference between gross precipitation and observed surface runoff.

Class 14: Unit **Hydrographs** 

If the phi-index of the storm is 0.5 inches per hour for 5 hours, then what is the net rainfall?



Class 14: Unit Hydrographs

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Class 14:

Unit Hydrographs



Class 14:

Unit Hydrographs



- DRO = Excess rainfall is the cumulative rainfall minus rainfall abstractions; estimates runoff volume (important for storage design)
- Influencing factors: rain amount, drainage area, soil type, ground cover
- Curve Number approach developed by Soil Conservation Service (now Natural Resources Conservation Service, or NRCS) to estimate daily excess rain amount from daily rain amount (we'll tackle this in week 8)

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Class 14: Unit Hydrographs

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Hydrograph Anatomy (components)

What is the Unit Hydrograph?

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Calculating Direct Runoff (DRO)



The Unit Hydrograph is a depiction of the hydrograph (discharge) that would result from 1.0 inch of rainfall.

The upshot: you normalize an observed hydrograph to produce the UH. Class 14: Unit Hydrographs

Learning Objectives

Hydrograph Anatomy (components)

What is the Unit Hydrograph?

How do you construct the Unit HG?

Calculating Direct Runoff (DRO)

1) Use DRO hydrograph to calculate total DRO ("trapezoidal rule")

2) Convert DRO hydrograph to Unit hydrograph: in this example, because total volume of DRO is 2 inches (2 inches x watershed area = volume), divide the ordinate (y-axis) values of discharge by 2, to normalize the values to a set of values that would produce only 1 inch of DRO -- this becomes the unit hydrograph.



Class 14: Unit Hydrographs

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Hydrograph Anatomy (components)

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Class 14: Unit Hydrographs

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Example: Develop Unit Hydrograph

#### In-Class Exercise: Unit Hydrograph Development



#### *In-Class Exercise: Unit Hydrograph Development*

For an 1850-acre watershed with a phi-index of 0.5 inches/hour, convert the following hydrograph into a 2-hour unit hydrograph:



The following are the essential steps for developing a unit hydrograph from a single storm hydrograph (see Fig. 2–7 and Example 2–3):

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- Check the volume of the unit hydrograph to make sure it is 1.0 in. (1.0 mm), and graphically adjust ordinates as required.

This example problem is example #2-1 on page 108 (Ch. 2) of Bedient....



A  $\sim$ 100 cfs baseflow is evident.

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- Check the volume of the unit hydrograph to make sure it is 1.0 in. (1.0 mm), and graphically adjust ordinates as required.



A ~100 cfs baseflow is evident - use constant discharge method.



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See spreadsheet for calculations....



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For a phi-index of 0.5 in/hour, subtract that from the hyetograph.



For a phi-index of 0.5 in/hour, subtract that from the hyetograph. This yields a net excess rainfall of 1 in/hour for 2 hours = 2 inches.



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1.

The following are the essential steps for developing a unit hydrograph from a single storm hydrograph (see Fig. 2–7 and Example 2–3):

Analyze the hydrograph and separate base flow (Section 2.3).

Time (hr)



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Measure the total volume of DRO under the hydrograph and convert this to inches (mm) over the watershed.

Convert total rainfall to rainfall excess through infiltration methods, such that rainfall excess = DRO, and evaluate duration D of the

Time (hr)

Time (hr)	Q (cfs)	Q-BF (cfs)	2-hr UH, Q
0	100	0	0
1	100	0	0
2	300	200	100
3	700	600	300
4	1000	900	450
5	800	700	350
6	600	500	250
7	400	300	150
8	300	200	100
9	200	100	50
10	100	0	0
11	100	0	0

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 Check the volume of the unit hydrograph to make sure it is 1.0 in. (1.0 mm), and graphically adjust ordinates as required.



Time (hr)

Based on the UH, what are (a)  $T_b$ , (b)  $t_p$ , and (c)  $t_c$ ?



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Convert total rainfall to rainfall excess through infiltration methods, such that rainfall excess = DRO, and evaluate duration D of the

a single storm hydrograph (see Fig. 2-7 and Example 2-3):

this to inches (mm) over the watershed.

Based on the UH, what are (a)  $T_b$ , (b)  $t_p$ , and (c)  $t_c$ ?



- Duration of rainfall excess (D): time from start to finish of rainfall excess
- Lag time (L or  $t_p$ ) : time from the center of mass of rainfall excess

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- Time of rise  $(T_R)$  : time from the start of rainfall excess to the peak of the hydrograph
- Time of concentration  $(t_c)$  : time for a wave (of water) propagate from the most distant pt in the watershed to the outlet. One estimate is time from the end of net rainfall to the inflection pt.
- Time base  $(T_b)$  : total duration of the DRO hydrograph

#### Based on the UH, what are (a) $T_b$ , (b) $t_p$ , and (c) $t_c$ ?

